#### CABLE REPEATER STATION DESIGN USING FIXED GAIN BLOCK PREAMPLIFIER AND POWERAMPLIFIER

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#### 1.0 Introduction

A cable repeater trunk amplifier station design in common use today consists of a flat (or nearly flat) frequency response, fixed gain preamplifier and poweramplifier, separated from each other and from the station input and output connectors by various loss networks. Refer to the block diagram in Figure 1.

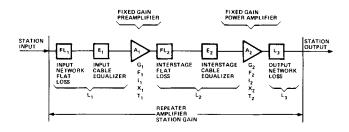


Figure 1. Repeater Station Block Diagram

The networks introducing loss provide the functions of cable equalization, gain and slope controls, bridging and AGC amplifier and power takeoff, and frequency division multiplex filters, all of which are necessary for cable repeater amplifier station performance. Apportioning the magnitude of loss in these networks in the station design should be done in a manner which, in the limit, allows the ultimate station noise figure to approach the value of the preamplifier  $(A_1)$  noise figure and the station distortion values to approach the values of the poweramplifier  $(A_2)$ distortion. Fixed gain amplifiers  $A_1$  and  $A_2$  will be referred to as IC (hybrid integrated circuit) amplifiers throughout the paper, although the analysis is general and applies to discrete component amplifiers as well.

The IC amplifier  $(A_1 \text{ and } A_2)$  distortion (crossmodulation, second order intermodulation distortion, and triple beat) is usually specified by IC vendors for signal carriers at equal signal levels. Equal signal levels are used for convenience in measurement and also provide a convenient reference.

The signal levels at the inputs and outputs of  $A_1$  and  $A_2$ in the repeater amplifier are normally not flat because of the cable attenuation frequency response and the cable system block tilt many times used. The magnitude and frequency response of the input, interstage, and output loss networks  $L_1$ ,  $L_2$  and  $L_3$ have very significant effects on the station noise and distortion performance. It is, therefore, difficult to predict and compare repeater amplifier station performance on the basis of various IC amplifier specifications based on flat level specifications. To solve this problem, a fast, simple means of predicting ultimate station performance from the known performance of IC amplifiers  $A_1$  and  $A_2$ , system block tilts, and station equalizer and loss network values has been developed by deriving a number of normalized performance degradation factors. This paper will define and explain the use of these degradation factors, and show the advantages to be gained by their use. The degradation factors, when added to the flat level IC specifications at a given station operating level, provide the station distortion and signal-to-noise ratio specifications. A list of symbols and definitions of terms used in the paper is listed on page 13.

Three amplifier design problems which inspired the derivation and use of the degradation factors are summarized in Table I. The derivation and use of the Degradation Factors provides a simple, quick means of solving the three problems listed below and summarized in Table I.

- 1. Determine station design from fixed gain IC amplifier specs to maximize station specs.
- 2. Determine fixed gain IC amplifier specs and station design to meet required station specs.
- 3. Determine station specs for a given station design and given fixed gain IC amplifier specs.

| Table I. Pro | blems Solved | with i | D-Factors |
|--------------|--------------|--------|-----------|
|--------------|--------------|--------|-----------|

|    | GIVEN                                     | DETERMINE  |
|----|---|--|
| 1. | IC Amplifier Specs                        | Station Design to Maximize Station<br>Performance Specs          |
| 2. | Station Performance<br>Specs              | IC Specs and Station Design to<br>Meet Station Performance Specs |
| 3. | Station Design, and IC<br>Amplifier Specs | Station Performance Specs  |

Ultimate station performance would be attained if the station noise figure were equal to the preamplifier noise figure  $F_1$ , and the station distortion were equal to or less than the poweramplifier distortion specifications I2, T2 and X2. The D-Factor derivation assumes that any distortion contributed by the preamplifier is additive on a voltage basis (20 log). The station distortion could be less than the poweramplifier (A<sub>2</sub>) distortion by the use of interstage distortion cancellation networks, particularly second order distortion. However, the distortion cancellation design approach is not in common use in present generation trunk station amplifier designs, and is not considered in this paper. Five D-Factor sets are derived for each particular trunk station design and level tilt. Each D-Factor is the number of dB that the trunk station performance deviates from the fixed gain IC amplifier specification measured at any flat level within the applicable dynamic range of the IC. This relationship is shown schematically in Figure 2.

The D-Factors ( $D_F$  and  $D_{S/N}$ ) are precisely accurate at each frequency calculated for station noise figure and signal-tonoise figure. The D-Factors ( $D_I$  and  $D_T$ ) are also accurate for the second order distortion product of each pair of frequencies calculated and each set of third order (triple beat) products calculated individually. The magnitude of the combination of second

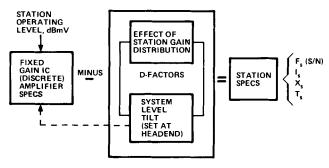


Figure 2. Relationship of IC Specs to Station Specs by D-Factors

and third order beats which occur at any single frequency for a given number of channels in the amplifier passband cannot be calculated in a practical way (Reference 6). The D-Factor  $(D_x)$  for crossmodulation in each channel calculated using the rule that "crossmodulation with n channels is [n-1] times that of a two channel measurement" is normally not accurate (Reference 9, 7) for broadband VHF amplifiers. A more precise answer for  $D_x$  can be obtained by measuring the actual fixed gain amplifiers with various block tilts and using these measured results as they apply to the calculation of  $D_x$ .

#### 2.0 IC Amplifier Characteristics

Fixed Gain IC amplifier parameters are summarized in Table II below. The numbers used are those listed in the published TRW data sheet for the CA100 (preamplifier) and CA200 (poweramplifier) IC amplifiers.

| Table II. Su | mmary of I | C Amplifier | Specifications |
|--------------|------------|-------------|----------------|
|--------------|------------|-------------|----------------|

|  | IC SPECIF                  | ICATION                      | STATION<br>SPECIFICATION                         |  |
|--|----------------------------|------------------------------|--|--|
| PARAMETER  | A <sub>1</sub><br>(preamp) | A <sub>2</sub><br>(poweramp) | CATV   |  |
| Gain (Fixed)   | G <sub>1</sub> = 16.3 dB   | G <sub>2</sub> = 16.3 dB     | G <sub>s</sub> = 22 dB (@ 300<br>MHz)            |  |
| Frequency Response   | Flat                       | Flat                         | Shaped to Equalize<br>Cable Loss                 |  |
| Noise Figure   | F <sub>1</sub> = 7.5 dB    | F <sub>2</sub> = 10 dB       | F <sub>s</sub> ≈ F <sub>1</sub> + D <sub>F</sub> |  |
| Distortion, Flat<br>Levels @ +50 dBmV                        |                            |                              |  |  |
| Intermodulation (2nd)<br>Order)(CH 2, 13, R)                 | l₁ =-68 dB                 | l <sub>2</sub> = -70 dB      | $I_s = I_2 = D_1$                                |  |
| Crossmodulation<br>(32 Channels)                             | X <sub>1</sub> = -52 dB    | X <sub>2</sub> =-57 dB       | $X_s = X_2 + D_x$                                |  |
| Triple Beat (3rd<br>order)(CH 3 + CH 4<br>+ CH A on 245 MHz) | T <sub>1</sub> =-73 dB     | T <sub>2</sub> = -78 dB      | $T_s = T_2 + D_T$                                |  |

To attain bandwidth, input and output match, repeatability, gain stability and minimum cost, an IC amplifier with the devices available today must have more than one stage. At this time, it is difficult to design IC amplifiers with responses which equalize the various types of cables in use. It is for these reasons that the IC preamplifiers and poweramplifiers available today have a flat frequency response and approximately 16 dB of gain.

#### 2.1 Fixed Gain Preamplifier

The preamplifier is designed for minimum attainable noise figure. The gain  $G_1$  is fixed at approximately 16 dB. Preamplifier IM  $(I_1)$  distortion, crossmodulation distortion  $(X_1)$ , and triple beat  $(T_1)$  is usually minimized by increasing the bias (which means more power consumption). An increase in bias tends to increase the preamplifier noise figure. Therefore, the trunk station designer should determine what preamplifier  $I_1$ ,  $T_1$  and  $X_1$  he must have so that both power consumption and preamplifier noise figure can be minimized.

The station noise figure  $(F_s)$  design goal is to achieve an  $F_s$  which is limited only by the noise figure  $F_1$  of the preamplifier. The station  $F_s$  is increased above  $F_1$  by the loss networks in the station and also by the poweramplifier noise figure  $F_2$ .

#### 2.2 Fixed Gain Poweramplifier

The station distortion design goal is to achieve station distortion  $(I_s, T_s \text{ and } X_s)$  which is limited only by the distortion of the fixed gain poweramplifier  $(I_2, T_2 \text{ and } X_2)$ . The gain  $G_2$  is fixed at approximately 16 dB. The IC poweramplifier is designed for minimum distortion  $(I_2, T_2 \text{ and } X_2)$  and its noise figure  $F_2$  is allowed to be higher than  $F_1$ . The minimum distortion is ultimately limited by the transistors (or active devices) used. The contribution of preamplifier distortion to the station distortion should be minimized by careful apportionment of the required loss networks in the station.

The station design challenge is to select the best compromise between conflicting requirements for the amount of loss apportioned to each loss network in the station (figure 1.0). Ultimate station noise figure should be limited by preamplifier noise figure and station distortion limited by poweramplifier distortion.

#### 3.0 Relating Station Performance Parameters to Fixed Gain Preamplifier and Poweramplifier Parameters by D-Factors

Even though the fixed gain amplifier specifications such as those listed in Table II for  $A_1$  and  $A_2$  are known, the station specifications obtainable are not immediately obvious. The various loss networks required in the station, as shown in Figure 1, make it impossible to attain station specifications which are as good as the  $A_1$  and  $A_2$  specifications. To further complicate the prediction of the station specifications from the known specifications of  $A_1$  and  $A_2$ , the station output level of each channel in the passband is normally not flat, but is tilted (block-tilted or linear-tilted).

A set of D-Factors<sup>1</sup> will be derived for a given set of station design requirements and system level tilts. The D-Factors are normalized such that they are independent of signal level. The fourth column of Table II lists the relationship between station and  $A_1$ ,  $A_2$  specifications by D-Factors. An outline of the station performance analysis leading to the D-Factors derivation and their use is shown in Figure 3. A station design example follows to show the type of results expected from the analysis. The numbers used are obtained from the analysis which follows later in the paper.

<sup>&</sup>lt;sup>1</sup>Because of the various functions required in a repeater amplifier station design, the station specifications will be worse than (or Degraded from) the Fixed gain  $A_1$  and  $A_2$  specifications; hence, the term D-Factor.

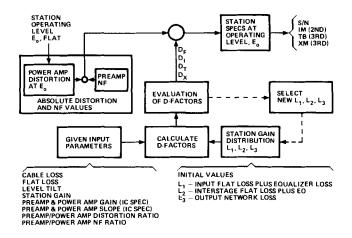


Figure 3. Station Performance Analysis Flow Diagram Using D-Factor Analysis

## 3.1 Design Example

## GIVEN PARAMETERS

| FIXED GAIN IC<br>AMPLIFIERS<br>(See Table II) |
|---|
| G <sub>1</sub> = 16.3                         |
| $G_2 = 16.3$                                  |
| $F_2 - F_1 = 2.5 dB$                          |
| $I_1 - I_2 = 2 dB$                            |
| $X_1 - X_2 = 5 dB$                            |
| $T_1 - T_2 = 5 dB$                            |
|   |
|   |
|   |

The D-Factors are calculated from the given parameters and the analysis procedures outlined in Figure 3 and derived in the following sections of this paper. The IC specs at +31 dBmVare summarized in the following table<sup>2</sup>. The D-Factors are added to the IC specifications to give the station specifications.

Note that the D-Factors are a function of frequency, so that D-Factors for a sufficient number of sets of frequencies are necessary to characterize the station performance across the passband of the amplifier. Note the difference of the station specs of column 4 versus the IC specs of column 2 in Table III.

The signal level of each channel applied to a station must be known in addition to the station noise figure  $F_s$  in order to determine the station signal-to-noise ratio (S/N). Since it is S/N and not N (noise) alone which is a measure of signal quality, an S/N degradation factor  $D_{S/N}$  is also derived. The operating signal levels in a system requiring a cascade of a number of repeater stations assume considerable importance. The relationship between channel levels, which will be defined by a number of level tilt settings, effect not only station S/N, but also the station distortion. The significance of level (block) tilts will be discussed in Section 6.0. Since the D-Factor  $D_{S/N}$  includes  $D_F$ , the  $D_F$  factor will be derived first, followed by the derivation of  $D_{S/N}$  in Section 5.0.

| Table III. | Station | Design | Example | Summary |
|------------|---------|--------|---------|---------|
|------------|---------|--------|---------|---------|

| Parameter | IC Specs (in dB)<br>@ +31 dBmV,<br>Flat Levels | D-FACTOR (in<br>dB) Calculated<br>from given Para-<br>meters Listed<br>Above | Station Specs (in<br>dB) @ +31 dBmV<br>& 4/2/0/0 Block<br>Tilt |
|-----------|--|--|--|
| NF        | F <sub>1</sub> (300 MHz)                       | D <sub>F</sub> (300 MHz)   | F <sub>s</sub> (300 MHz)                                       |
|           | = 7.5  | = 2.8  | = 10.3   |
|           | F <sub>1</sub> (Chan 2)                        | D <sub>F</sub> (Chan 2)  | F <sub>s</sub> (Chan 2)  |
|           | = 6.5  | = 12.8   | = 19.3   |
| S/N       | Input Level at<br>300 MHz is +9<br>dBmV        | D <sub>S/N</sub> (300)=-2.7<br>D <sub>S/N</sub> (Chan 2)<br>=-2.0            | S/N (300 MHz)<br>=+57.8<br>S/N (Chan 2)<br>=+58.5              |
| ١M        | I <sub>2</sub> (CH 2 + 13                      | D <sub>1</sub> (CH 2 + 13 in   | I <sub>s</sub> (CH 2 + 13 in                                   |
|           | R) =-89  | R) = 3.4   | R) =-85.6  |
| ТВ        | T <sub>2</sub> (CH 3 + 4 + A                   | D <sub>T</sub> (CH 3 + 4 + A)  | T <sub>s</sub> (CH 3 + 4 + A)                                  |
|           | in Ch 0) = -116                                | =-3.8  | =-119.8  |
| ХМ        | X <sub>2</sub> (CH 2, 32<br>Channels) =-95     | D <sub>x</sub> (CH 2) = 4.1  | X <sub>s</sub> (CH 2) =-90.9                                   |

4.0 Normalized Preamplifier Noise Figure Degradation,  $D_F$ It has been previously stated that the ideal station noise figure (F<sub>s</sub>) would be equal to the fixed gain preamplifier noise figure (F<sub>1</sub>). In other words,  $D_F$  would be equal to zero in equation 4.1.

(4.1)  $F_s = F_1 + D_F$ 

The magnitude of  $D_F$  is a function of the following:

- 1. Input network loss (flat and sloped).
- 2. Interstage network loss (flat and sloped).
- 3. Poweramplifier to preamplifier noise figure ratio.

The input and interstage network losses are in part determined by  $G_1$ ,  $G_2$ , and the station gain  $G_s$ . The magnitude of  $D_F$  will be different at maximum  $G_s$  compared to operating  $G_s$ . The noise figure  $F_1$  of  $A_1$  and  $F_2$  of  $A_2$  is normally a smooth function of frequency with today's devices, and is about 1.2 dB higher at 300 MHz compared to its value at 55 MHz. Also,  $L_1$  and  $L_2$  are functions of frequency, so that  $D_F$  is a function of frequency.

The noise figure at the IC preamplifier input terminals will be calculated first. The effect of input loss networks on the station noise figure will then be added to this result. Lower case symbols indicate numeric values and capital letters indicate dB values. The noise figure is independent of signal level and block tilt.

Referring to Figure 4, the expression for  $f_1$  is

(4.2) 
$$\dot{f_1} = f_1 + \frac{\dot{f_2} - 1}{g_1}$$

<sup>&</sup>lt;sup>1</sup>Level Tilt notation defined in Section 6.0.

 $<sup>^2</sup> This example assumes an IC distortion characteristic for which relative third order distortion (Crossmodulation and triple beat) decreases 2 dB for every 1 dB of level reduction and relative second order distortion decreases 1 dB for every 1 dB of level reduction. Note that the <math display="inline">A_1$  and  $A_2$  distortion versus level characteristic must be defined in order to obtain a valid  $I_s, T_s$  and  $X_s.$ 

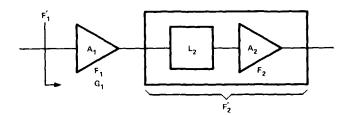


Figure 4. Block Diagram of Amplifiers Cascaded & Separated by Loss

The value of interstage loss  $L_2$  is determined by  $G_8$ ,  $G_1$ , and  $G_2$  and the apportionment of loss between  $L_1$ ,  $L_2$  and  $L_3$ .  $L_2$  adds to the noise figure  $F_2$  on a dB for dB basis so that

(4.3) 
$$F_2 = F_2 + L_2$$
 in dB

The quantity  $1_2$  is the numeric gain (loss) of the interstage network and is less than 1.0. Equation 4.2 becomes

(4.4) 
$$f'_1 = f_1 + \frac{(f_2/l_2) - 1}{g_1}$$

By factoring out  $f_1,$  the effect of  $f_2$  and  $1_2$  on  $f_1^{'},$  the total noise factor, can be shown

(4.5) 
$$f_1' = f_1 \left[ 1 - \frac{1}{f_1 g_1} + \frac{f_2}{f_1 g_1 I_2} \right]$$
 Numeric

(4.6) 
$$f'_1 = f_1 \left[ \frac{f_1 g_1 - 1}{f_1 g_1} + \frac{k}{g_1 I_2} \right]$$
 Numeric

The ratio of  $f_2/f_1$ , denoted k, is normally greater than one, which means that the power amplifier noise factor has the effect of increasing  $f_1$  as shown in equation 4.6. It is assumed here, without loss of generality, that  $F_1$  versus frequency and  $F_2$  versus frequency have the same relative values versus frequency. Since  $f_1g_1 >>1$  for most practical cases, equation 4.6 can

be written

(4.7) 
$$\mathbf{f}'_1 = \mathbf{f}_1 \left[ \mathbf{1} + \frac{\mathbf{k}}{\mathbf{g}_1 \mathbf{1}_2} \right]$$
 Numeric

Equation 4.7 is a very important result. The interstage loss  $1_2$  is a number less than one. The higher the interstage loss, the smaller  $1_2$  and the larger  $f_1$  becomes. Written in dB

(4.8) 
$$F'_1 = 10 \log f_1 + 10 \log \left[1 + \frac{k}{g_1 I_2}\right]$$

The factor  $D'_F$  is defined as the degradation of the preamplifier noise figure looking into the preamplifier (A<sub>1</sub>) input terminals. It is a function of preamp gain, interstage loss; and the f<sub>2</sub>/f<sub>1</sub> ratio.

(4.9) 
$$D'_{F} = 10 \log \left[1 + \frac{k}{g_1 l_2}\right]$$

Preamplifier noise figure degradation as a function of interstage loss and  $A_2$  to  $A_1$  noise figure ratio is summarized in Table IV. Note that each dB of  $A_2$  noise figure increase relative to  $F_1$  is equivalent to a dB increase in interstage loss. Also note that the quantity  $1_2$  is a function of frequency.

| Table IV. | Noise Figure Degradation for Diagram Shown in        |
|-----------|--|
| Fi        | gure 4.0 (Calculated Using $G_1 = 15.5 \text{ dB}$ ) |

| INTERSTAGE<br>LOSS $L_2$ in dB<br>(at a Specific Frequency) | $\begin{array}{l} PREAMPLIFIER \\ ,\\ NOISE FIGURE DEGRADATION, D_F \\ (K=F_2 \sim F_1 \text{ in } dB) \end{array}$ |      |      |      |
|---|---|------|------|------|
|   | K=0   | K=2  | K=4  | K≈6  |
| 2   | .17   | .28  | .44  | .69  |
| 4   | .28   | .44  | .69  | 1.06 |
| 6   | .44   | .69  | 1.06 | 1.59 |
| 8   | .69   | 1.06 | 1,59 | 2.31 |
| 10  | 1.06  | 1.59 | 2.31 | 3.26 |
| 12  | 1.59  | 2.31 | 3.26 | 4.43 |
| 14  | 2.31  | 3.26 | 4.43 | 5.81 |
| 16  | 3.26  | 4.43 | 5.81 | 7.37 |

The noise figure degradation factor  $D'_F$  for k = 0, 2, and 4 is plotted in Figure 5 versus interstage attenuation.

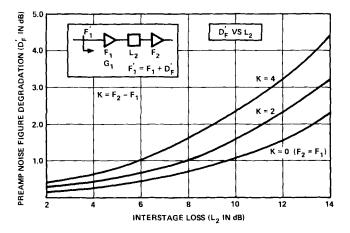


Figure 5.  $D_F$  vs  $L_2$  (Interstage Loss) for  $G_1 = 15.5$  dB

The station noise figure  $F_s$  is equal to  $F_1$  in dB increased by the amount of loss of the input network (input equalizer loss plus flat loss).

(4.10) 
$$F_s = F_1 + 10 \log \left[1 + \frac{k}{g_1 I_2}\right] + L_1$$
 in dB

The normalized preamplifier noise figure degradation factor  $\mathrm{D}_{\mathrm{F}}$  , for the station, is therefore

(4.11) 
$$D_F = 10 \log \left[ 1 + \frac{k}{g_1 I_2} \right] + L_1$$
 in dB

The preamplifier noise figure degradation factor  $D_F$  is plotted in Figure 6 versus frequency for two different input equalizers, at operating station gain, and at maximum gain for an  $E_1$  of 14 dB.

# 5.0 S/N Degradation Factor Derivation (DS/N)

In an amplifier cascade design in which the amplifier gain at each frequency offsets the loss of the cable at each frequency - i.e., a unity gain system, the repeater station noise figure, input signal level (function of frequency), and the number of amplifiers in cascade define the cascade signal-to-noise (S/N) ratios.

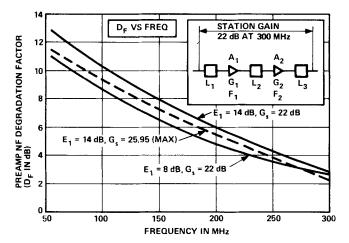
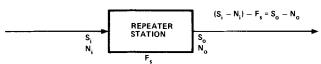


Figure 6. D<sub>F</sub> versus Frequency using Design Example Parameters



 $F_s$  IS STATION NOISE FIGURE AND IS FREQUENCY DEPENDENT. S, IS THE INPUT LEVEL TO THE STATION AND IS FREQUENCY DEPENDENT.

#### Figure 7. Station S/N

The signal to noise ratio of an N amplifier cascade, assuming identical amplifiers, is:

$$S_i - N_i = S_i - [-59 + F_s + 10 \log_{10}N]$$
 in dB

(5.1) 
$$S_i - N_i = 59 + S_i - F_s - 10 \log_{10} N$$
 in dB

-59 dBmV is the thermal noise threshold for a 4 MHz bandwidth in a 75 ohm system at  $20^{\circ}$ C.

For convenience, the S/N of a single station is analyzed and the results presented for a single station only. The  $10 \log N$ factor can be added later for specific system cascade lengths. The single station S/N is:

$$(S_i - N_i) = 59 + S_i - F_s$$

An S/N degradation factor is derived which serves a number of purposes. It is used to calculate station S/N as a function of station gain distribution and IC amplifier  $(A_1)$  noise figure. It normalizes the noise figure  $F_1$  versus frequency characteristics of preamplifier  $A_1$  to the highest frequency channel value. It normalizes the input signal  $S_i$  to the highest channel frequency signal level so that system analysis for all channels uses only this one signal level. The signal level normalization accounts for the cable loss versus frequency response and for the block tilt used.

The S/N degradation factor is denoted as  $D_{S/N}$  and is a function of the following:

- 1. frequency
- 2. cable loss and cable system flat loss
- 3. F<sub>1</sub> versus frequency variation
- 4. poweramplifier to preamplifier noise figure ratio
- 5. interstage loss (flat and sloped)
- 6. input network loss (flat and sloped)
- 7. output network loss
- 8. block tilt
- 9. preamplifier and poweramplifier gain
- 10. station gain

The single repeater station S/N equation using the S/N degradation factor has the form:

(5.2) 
$$S_i - N_i = 59 + S_i (at 300 MHz) - F_1 (300 MHz)$$

 $S_i$  is the input signal level in dBmV at the highest frequency, which for this analysis is 300 MHz.

 $\mathbf{F}_1$  is the noise figure of the IC preamplifier at 300 MHz.

 $D_{S/N}$  is the signal to noise ratio degradation factor and is equal to  $D_F$  plus a level normalization factor, a noise figure normalization factor and a block tilt factor,  $B_F.$ 

Figure 8 shows the general shape that input levels to a repeater station will have for flat level (solid curve) operation and block tilted level (dashed curve) operation. Reducing levels of lower frequency channels by block tilting levels lowers the S/N of these channels, but it will be shown in the sections on station distortion analysis that station distortion performance is improved. Block tilting levels provides a compromise between station S/N ratio on all channels and station distortion performance. Equation (5.3) defines  $D_{S/N}$ :

(5.3) 
$$D_{S/N} = -10 \log \left[1 + \frac{k}{g_1 I_2}\right] - L_1 + \Delta A + B_F$$

Where  $\Delta A$  is the difference in level in dB for each carrier frequency station input level compared to the station input level at 300 MHz. B<sub>F</sub> is the number of dB which must be subtracted from each channel for a given block tilt, compared

to flat level operation.

The last two terms added to the expression for  $D_{S/N}$ ,  $\Delta A$  and  $B_F$ , could have been omitted since the effect they produce is taken into account in the  $S_i$  term of equation (5.1). However, by including them in the  $D_{S/N}$  factor, the  $S_i$  term becomes a constant defined at one frequency. Since the  $D_{S/N}$  factor contains other terms which vary with frequency, it is convenient to combine the  $\Delta A$  and  $B_F$  terms with the  $D_F$  term. The term  $\Delta A$  is positive and thereby increases the S/N. The term  $B_F$  will either be negative or zero at channel frequencies across the band. The cable system S/N will be highest when  $D_{S/N}$  is most positive.

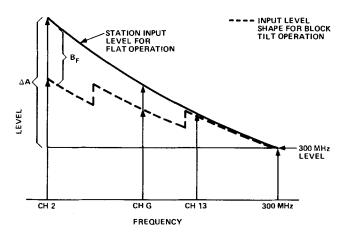


Figure 8. Station Input Level Relationships

# 5.1 Example of D<sub>S/N</sub> Application

The values of  $D_{S/N}$  plotted in Figure 9 were calculated using the design parameters given in Section 3.0. The  $D_{S/N}$  for flat level (0/0/0/) operation is plotted in Figure 9a, and a block tilt level (4/2/0/0) condition in Figure 9b. A set of  $D_{S/N}$  values for input equalizer values of 8 dB and 14 dB is shown in each figure. Values of  $D_{S/N}$  for Channels 2, 6, and 13 for two level tilt conditions and two input equalizer values are taken from the curves shown in Figure 9 (a & b) and listed in the table below. Also listed in the table are station S/N for an A<sub>1</sub> noise figure of 7.5 dB (300 MHz) and S<sub>i</sub> (input level @ 300 MHz) of +9 dBmV. The S/N is evaluated from equation 5.2.

| 5.2 $S_i - N_i = 59 - F_1 (300 \text{ MHz}) + S_i (300 \text{ MHz})$ | $00 \text{ MHz} + D_{S/N}$ |
|--|----------------------------|
|--|----------------------------|

|   | CHANNEL | Level Tilt 0/0/0/0<br>Input EQU=14 dB |      | Level Tilt 4/2/0/0<br>Input EQU=8 dB |      |
|---|---------|---------------------------------------|------|--------------------------------------|------|
| Γ |         | D <sub>S/N</sub>                      | S/N  | D <sub>S/N</sub>                     | S/N  |
|   | 2       | 1.98                                  | 62.5 | 14                                   | 60.4 |
|   | 6       | 1.38                                  | 61.9 | 83                                   | 59.7 |
|   | 13      | 1.09                                  | 59.4 | ~.14                                 | 60.4 |
|   |         |                                       |      |                                      |      |

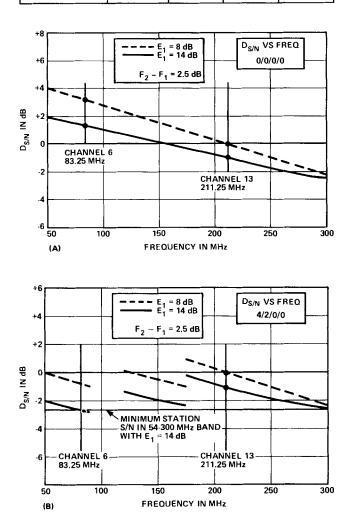


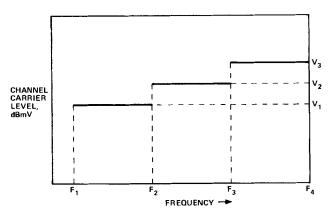
Figure 9. Comparison of D<sub>S/N</sub> versus Frequency For Two Level Tilts and Two Different Input Equalizers

The station design with a 14 dB input equalizer and operation with flat levels results in a better S/N (62.5 versus 60.4) at Channel 2 and worse S/N (59.4 versus 60.4) at Channel 13 than the station design with an 8 dB input equalizer and block tilted 4/2/0/0 levels. Choice of level tilt obviously has a significant effect on station S/N.

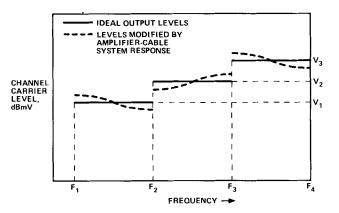
The system operator has some leeway in selecting a trunk station level tilt, but before deviating from the station manufacturer's recommended level tilt values, he must understand the consequences on the station S/N and distortion parameters.

#### 6.0 Signal Level Relationships (Block Tilts)

The amplifier cascade design is a unity gain design. The gain of each repeater amplifier station at each frequency in its passband is set to exactly offset the loss which precedes it. Therefore, the relationship between levels at each frequency in the passband at the output of each repeater station will be identical to the level relationship set at the headend, modified only by the response flatness of the amplifier cascade. An example is shown in Figure 10.



(A) HEADEND OUTPUT LEVELS, BLOCK TILTED



(B) REPEATER STATION OUTPUT LEVELS, BLOCK TILTED

#### Figure 10.

The level at the repeater station output normally refers to the levels of the channel carriers in the highest frequency band block. In Figure 10, the level V<sub>3</sub> for channel carriers between frequencies  $f_3$  and  $f_4$  is referred to as the operating level of the station. The passband of the amplifier of Figure 10 is  $f_4 - f_1$  and is divided into three frequency bands of blocks,  $f_4 - f_3$ ,  $f_3 - f_2$ , and  $f_2 - f_1$ . When the level of each of the bands or blocks of carrier frequencies is set to a constant level, the levels are described as "block-tilted". Choice of the magnitude of difference in levels between frequency blocks  $(V_3 - V_2 \text{ and } V_2 - V_1)$  and number of blocks is based on obtaining the result which gives the best compromise to maximize system S/N and minimize system distortion. A given repeater amplifier design may dictate the use of a specific block tilt to be used in order to optimize system performance. However, many times enough station performance margin is available so that the choice of a number of different "block tilts" can be used with a given repeater station design without sacrificing system performance.

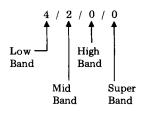
The most important reason for selecting and operating with amplifier station output levels which are not equal at each frequency in the passband is that the amount of signal power at the station output can be reduced. Less signal power results in many lower magnitude distortion products, although some distortion product magnitudes will increase. Offsetting the advantage of reduced level of distortion products by use of a level tilt is a decrease in signal-to-noise ratio on those channels at reduced levels. However, consider that the level of channel 2 carrier frequency is attenuated by the cable approximately 13 dB less than a carrier frequency at 300 MHz for 22 dB spacing at 300 MHz. Therefore, reducing the levels of the low frequency channels can be down without reducing the S/N of low frequency channels relative to higher frequency channels. Also, the noise figure of the active amplifying devices have somewhat lower noise figures at lower frequencies relative to higher frequencies.

#### 6.1 Shorthand Notation for Block Tilts in Use

The frequency band from 54 to 300 MHz is commonly divided into four bands.

| Low band   | 54-88 MHz   | CH 2-6    | 5 channels  |
|------------|-------------|-----------|-------------|
| Mid band   | 120-174 MHz | CH A-I    | 9 channels  |
| High band  | 174-216 MHz | CH 7-13   | 7 channels  |
| Super band | 216-300 MHz | CH J-CH W | 14 channels |

Using the superband block of frequencies for the reference level, the block tilt (shorthand) notation takes the form:



The high band levels are the same as the super-band levels, mid-band levels are 2 dB below the super-band levels, and low-band levels are 4 dB below super-band levels. A summary of block tilts specified for trunk stations taken from a number of manufacturers' data sheets in the past year are summarized in Table V.

Table V. Examples of Block Tilts Published in Manufacturer's Data Sheets

| COMPANY            | BLOCK TILT              |
|--------------------|-------------------------|
| Anaconda           | 4/2/0/0                 |
| Jerrold            | 3/3/0/0                 |
| Theta-Com          | 7/4/2/0                 |
| Scientific Atlanta | 4/2/2/0                 |
| Magnavox           | 0/0/0/0 (No block tilt) |

# 6.2 General Comments on Distortion Product Accumulation in Broadband VHF Amplifiers.

Care must be exercised in attempting to analytically predict second order intermodulation product, triple beat (third order) product, and crossmodulation product accumulation in a single channel in a broadband VHF amplifier as a function of channels and amplitudes of individual channels. The only practical way to evaluate the cumulative distortion products of an amplifier station is by measurement. However, calculation of the magnitude of single second and third (triple beat) order beat products can be done precisely, and thereby provide considerable insight into the station design.

For reasons pointed out in both references 6 and 7, broadband VHF amplifiers used in CATV repeater stations have transfer characteristics which in general, invalidate the rule that "n channel crossmodulation distortion is n-1 times the 2 channel crossmodulation value". However, because measurement on a fixed gain amplifier in common use today does follow the "n-1 rule" for crossmodulation accumulation in channel 2 for trunk station application, a  $B_x$  factor for channel 2 is analytically derived. Obtaining a  $B_x$  factor must normally be done by measurement first, followed by analysis. Table VI contains a summary of the methods of analysis for these types of distortion products.

| Table VI. | Amplifier Distortion Characteristics |
|-----------|--------------------------------------|
|           | Analysis Methods                     |

| METHOD OF<br>ANALYSIS                        |
|--|
| Analytical<br>Measurement in Each<br>Channel |
| Ahalytical<br>Measurement in Each<br>Channel |
| Measurement in Each<br>Channel<br>Analytical |
|  |

## 6.3 Second Order IM (A ± B) Block Tilt Factor, BI

A flat gain amplifier operated with a pair of equal level signals produces second order beats (A + B and A - B) which, if in the passband of the amplifier, interfere with a third signal. The ratio of second order beat to the signal for flat output levels is different than the ratio obtained when the amplifier is operated with linear or block tilted levels. The difference in second order IM ratio (in dB) resulting for tilted level operation versus flat level operation for the same amplifier is defined by a block tilt factor B<sub>I</sub>. Values of B<sub>I</sub> for six pairs of channel carrier frequencies and three level tilts are summarized in Table VI.

As an example, for the numbers listed in Table VII, the 2nd order IM product of Channel 13 minus (-) Channel G producing a beat which interferes with Channel 2 is 2 dB worse when operating with a 4/2/0/0 block tilt than with no block tilt (0/0/0/0) or flat levels. However, the IM ratio for the Channel 2 plus (+) Channel G beat in Channel 13 provides a 6 dB improvement for the 4/2/0/0 block tilt condition.

The magnitude of the combination of total number of second order beats occurring at a specific frequency for a specific system application and given number of channels can practically be determined by measurement only. Second order product addition depends on magnitude *and phase* of each product.

 Table VII.
 Block Tilt Factor B<sub>1</sub> For Six Pairs of Channel Carrier

 Frequencies and Three Block Tilts.

| RELATIVE IM DISTORTION |         | LT FACTOR |         |
|------------------------|---------|-----------|---------|
| PRODUCT (TV CHANNELS)  | 4/2/0/0 | 3/3/0/0   | 0/0/0/0 |
| R – 13 (in Ch 2)       | +4      | +3        | 0       |
| 13 – G (in Ch 2)       | +2      | 0         | 0       |
| 13 – 2 (in Ch G)       | -2      | 0         | 0       |
| 2 + G (in Ch 13)       | -6      | 6         | 0       |
| 13 + 2 (in Ch R)       | -4      | -3        | 0       |
| R - 2 (in Ch 13)       | -4      | -3        | 0       |

#### 6.4 Third Order [Triple Beat (A $\pm$ B $\pm$ C)] Block Tilt Factor, BT

The B<sub>I</sub> factor is calculated considering the level difference of two frequencies and the level difference between that of the beat frequency and that of the frequency with which it interfaces. The B<sub>T</sub> factor is calculated in a similar manner, except that the level difference of three frequencies rather than two frequencies is accounted for. A third order IM (2A  $\pm$  B) factor could also be calculated, but is not included in this paper.

Triple beat products are considered to be a limiting parameter in 30+ channel systems with today's amplifiers. One complication of the triple beat problem is the sheer number of possible products for 30+ channel operation. It is therefore naive to assume that the calculation of a few triple products define an amplifier station's triple performance. However, calculation of the triple beat product amplitude for a few products for a given level tilt relative to flat level operation will indicate a trend, indicating whether triple beat magnitude reduction is possible by the use of level tilts. A more useful and detailed analysis of this problem must be reserved for another paper.

 $B_T$  factors for a few triple combinations and level tilt conditions are summarized in Table VIII.

| Table VIII. | Triple Beat Block Tilt Factors as Function of |
|-------------|---|
|             | Block Tilt                                    |

|   | TRIPLE BEAT PRODUCTS<br>LISTED BY CHANNEL<br>COMBINATIONS | TRIPLE BEAT BLOCK TILT FACTOR<br>B <sub>T</sub> IN dB<br>4/2/0/0 0/0/0/0 3/3/0/0 |   |    |
|---|---|--|---|----|
|   |   |  |   |    |
|   | 3 + 4 + A in 0  | -10  | 0 | -9 |
| 1 | A – J + Q in 5  | +2   | 0 | 0  |
| ł | G + S – J in 13   | -2   | 0 | -3 |
|   | 13 + R – J in Q   | 0  | 0 | 0  |
| Į | 7 – 13 + L in G   | +2   | 0 | +3 |

A negative number in the table indicates a lower amplitude beat at the station output compared to flat level operation and a positive number indicates that the triple beat product for that specific three channel beat product is higher (or worse) than that resulting with flat level operation.

#### 6.5 Crossmodulation Block Tilt Factor, B<sub>x</sub>

The effect of tilted levels and fixed gain preamplifier crossmodulation distortion contribution for a given number of channels must be known in order to determine station XM from the given flat level XM specification of the fixed gain preamplifier and poweramplifier. Remembering the precautionary comments of Section 6.2, and applying the "n-1 XM accumulation" rule, a  $B_x$  factor for channel 2 is derived. The station level tilt factor,  $B_x$ , defines the difference between the XM produced with flat levels, compared to the XM expected with tilted levels for a given number of channels in a given channel. The  $B_x$  term is then included in the XM D-factor,  $D_x$ , for a given station design.

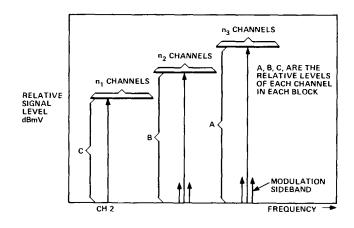


Figure 11. Block Tilted Levels Versus Frequency

The crossmodulation at the level of channel 2 for block tilted levels compared to flat levels is given by equation 6.5.1 (assuming equal modulation percentage on each modulated channel.)

(6.5.1) 
$$m_2 = \frac{(n_1 - 1) + n_2 (b/c)^2 + n_3 (a/c)^2}{n - 1}$$
 Numeric

where  $n_1 + n_2 + n_3 = n$  (total number of channels)

To obtain the  $B_x$  factor for channel 2 compared to flat level operation at level A (which would be the flat level condition):

(6.5.2)  $B_x$  (Channel 2) = 20 log (m<sub>2</sub>) - (A-C)

As an example of the use of equation 6.5.2, consider the following:

Seven high band channels at level A, 5 dB above five (5) low band channels at level C.

$$n_1 = 5, n_3 = 7, A/C = 10 \exp(5/20) = 1.79$$

Substituting these values in (6.5.1)

$$m_2 = \frac{(5-1)+7(1.79)^2}{(12-1)} = \frac{4+22.4}{11} = 2.4$$

Evaluating equation 6.5.2

 $B_x$  (Channel 2) = 20 log (2.4) - 2 (5) = -2.4 dB

Operating with 12 channels, 5 of the channels 5 dB below level A, results in channel 2 XM 2.4 dB below the XM value of channel 2 when all 12 channels are at level A.

Using equations 6.5.1 and 6.5.2, the  $B_x$  factor for channel 2 is calculated and summarized in the table for a number of block tilt and number of channel conditions:

| 12 CHANNÉLS   |              |          |              |       |                        |
|---------------|--------------|----------|--------------|-------|------------------------|
|               | LOW          |          | HIGH         |       | B <sub>x</sub><br>CH 2 |
| No. Chan.     | 5            |          | 7            |       |                        |
| Relative Lev. | 3 dB<br>5 dB |          | 0 dB<br>0 dB |       | ~1.7 dB<br>-2.5        |
|               | 2            | 1 CHAN   | NELS         |       |                        |
|               | LOW          | MID      | HIGH         |       |                        |
| No. Chan.     | 5            | 9        | 7            |       |                        |
| Relative Lev. | -3<br>-5     | -3<br>-2 | 0<br>0       |       | -3.4<br>-3.1           |
| 35 CHANNELS   |              |          |              |       |                        |
|               | LOW          | MID      | HIGH         | SUPER |                        |
| No. Chan.     | 5            | 9        | 7            | 14    |                        |
| Relative Lev. | -3<br>-4     | -3<br>-2 | 0            | 0     | -1.8<br>-1.6           |

#### Table IX. XM Block Tilt Factor B<sub>x</sub> (Calculated using n-1 rule.)

# 7.0 Normalized Poweramplifier Second Order IM Distortion Degradation Factor, DI

The quantity  $D_I$  is derived so that repeater station 2nd order IM distortion as a function of station gain distribution and block tilt can be easily related to the flat level IC preamplifier and poweramplifier IM distortion specifications. One  $D_I$  is calculated for each A + B and/or A – B product considered necessary to define the station IM performance across the passband.

$$(7.1) \quad I_s = I_2 + D_I \qquad \text{in dB}$$

The quantity  $I_s$  is the relative 2nd order IM for a pair of frequencies interfering with a third frequency at the station output. The quantity  $I_2$  is the relative 2nd order IM ratio in dB for the same pair of frequencies at equal levels at the poweramplifier output.

D<sub>I</sub>, the degradation factor, is independent of the absolute station output signal levels and is a function of the following:

- 1.0 Preamplifier IM distortion relative to poweramplifier distortion.
  - 2.0 Preamplifier gain and poweramplifier gain.
  - 3.0 Interstage network loss (flat and sloped), a function of station gain
  - 4.0 Block tilt.

Two assumptions are made in the derivation of  $D_I$  which do not affect the result in general. First, the IM distortion specification for each pair of frequencies of the flat preamplifier is assumed to be related to the IM distortion specification for the same pair of frequencies of the flat poweramplifier by a constant number of dB. Second, the IM distortion of the preamplifier is assumed to add in phase with the IM distortion of the poweramplifier. This represents a worst case condition for the total IM distortion of the repeater station. Second order IM addition is phase and amplitude sensitive so that in the actual hardware design, some degree of cancellation will occur, either by accident or by design.

In the following analysis, lower case letters indicate numeric, and upper case letters indicate dB. The total repeater station IM distortion for a given pair of signals is the sum of the IM distortions generated by all sections of the amplifier. Assuming that the only sources of IM distortion products are the preamplifier and poweramplifier, then the station distortion is:

$$(7.2) \quad 20 \log_{10} (i_1 + i_2) = 20 \log_{10} [i_2 (1 + i_1/i_2)]$$

 $i_1 = 10 \exp (I_1/20)$  Preamplifier IM distortion

 $i_2 = 10 \exp (I_2/20)$  Poweramplifier IM distortion

The terms  $I_1$  and  $I_2$  represent the second order distortion ratio in dB for a given pair of frequencies as measured for the preamplifier and poweramplifier with flat output levels. Modification to the IM ratios for block tilt operation compared to flat level will be added later.

(7.3) The station second order IM distortion can be written as:

| $I_s = \underbrace{20 \log (i_2)}_{+} +$ | $20 \log (1 + i_1/i_2)$  |
|--|--------------------------|
| Poweramplifier                           | IM Distortion Con-       |
| IM Distortion                            | tributed by Preamplifier |

The numeric ratio  $(i_1/i_2)$  may be solved by working with the amplifier constants in dB, since the numeric ratio can be written:

$$(7.4)$$
  $i_1/i_2 = 10 \exp (I_1 - I_2)/20$ 

where  $I_1$  and  $I_2$  are in dB.

The difference between preamplifier and poweramplifier IM as measured with flat levels at the same level, is assumed equal to a constant D.

(7.5)  $D = I_1 - I_2$  in dB (a positive number).

The quantity D is usually positive, since the preamplifier IM distortion is normally worse (less negative) than the poweramplifier IM distortion. If D = 0 dB, the preamplifier IM distortion is equal to the poweramplifier IM distortion.

Relative second order IM distortion is proportional to signal level, i.e., two signals whose levels are each changed by 1 dB produce a relative IM product change of 1 dB. As an example and to prepare for the analysis which follows, consider a poweramplifier with flat output levels preceded by a flat loss network and a flat output preamplifier, as shown in Figure 12.

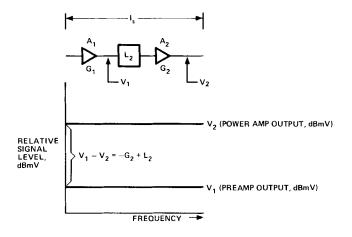


Figure 12. Flat Output Preamplifier and Poweramplifier

The ratio of preamp  $(A_1)$  to poweramp  $(A_2)$  distortion can be written:

(7.6) 
$$(I_1 - I_2) = (V_1 - V_2) + D$$
  
Due to level Due to IM  
difference of difference of  
 $A_1$  and  $A_2$  A1 and A2

The preamp  $(A_1)$  output level  $V_1$  is  $G_2$  dB below the poweramp  $(A_2)$  output level  $V_2$  increased by the interstage loss  $L_2$ . Equation 7.6 can then be written as:

$$(7.7) \quad (I_1 - I_2) = -G_2 + L_2 + D \qquad \text{in dB}$$

The station distortion  $I_{\text{s}}$  shown in Figure 12 can then be written:

(7.8) 
$$I_s = I_2 + 20 \log \left[ 1 + 10 \exp \left[ (I_1 - I_2)/20 \right] \right]$$
  
Degradation of Poweramp IM Distortion Spec

In a cable repeater station, neither amplifier  $A_1$  or  $A_2$  may operate with flat levels. The poweramp  $(A_2)$  may operate with a level tilt, which has been set at the cable system headend, and the preamp  $(A_1)$  levels will be sloped as a result of cable equalization in the station.

It has been instructive to solve the flat level  $A_1$ ,  $A_2$ , and  $L_2$  problem described by equation (7.7). Using this equation as a building block, the final solution is obtained by the following procedure:

Step 1: Solve for the station  $(I_1 - I_2)$  ratio by considering the actual frequency response of the preamp  $A_1$  output levels. The amount of cable loss, and cable equalization placed before the preamp  $A_1$  will define this level relationship, which is sketched in Figure 13. The term  $L_2$  in equation (7.7) must be modified to account for the sloped levels at preamp  $A_1$  output. If the term  $L_2$  in equation (7.7) is the interstage insertion loss at the frequency which is interfered with by the IM product, then a term  $\Delta L$  must be added to the equation to account for the level differences of the frequencies at the preamp output.

Equation 7.7 now becomes:

(7.9) 
$$(I_1 - I_2) = -G_2 + L_2 + \Delta L + D$$
 in dB

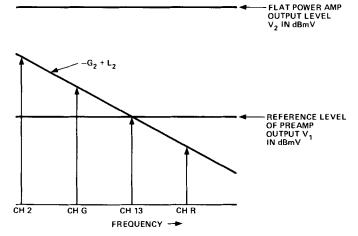


Figure 13. Sloped  $A_1$  Output Levels When  $A_2$  Output Levels are Flat

Step 2: Substitute the value of  $(I_1 - I_2)$  defined by equation (7.9) in 7.8, add the system block tilt factor  $B_I$ , and add  $L_3$  which is any loss between  $A_2$  output and station output terminals (connector).

The station IM ratio for a given pair of frequencies is then

(7.10) 
$$I_s = I_2 + \underbrace{20 \log \left[1 + 10 \exp \left(\frac{(I_1 - I_2)}{20}\right)\right] + B_I + L_3}_{Dr}$$

The difference between station IM distortion and  $A_2$  IM distortion for a given pair of frequencies is then:

(7.11) 
$$D_I = 20 \log \left[ 1 + 10 \exp \left( \frac{(I_1 - I_2)}{20} \right) \right] + B_I + L_3 \text{ in } dB$$

where  $(I_1 - I_2)$  is determined by evaluating equation (7.9) for a given set of station design parameters.

Using  $A_1$  and  $A_2$  specifications and station design parameters given in Section 3.0, equation (7.11) was evaluated and the results plotted in Figure 14 for a flat level system and Figure 15 for a block tilt (4/2/0/0) system. The  $D_{S/N}$  factor for channels 2, G, and 13 are also included in Figures 14 and 15 to show the relationship between  $D_I$  and  $D_{S/N}$  as a function of input equalizer value. Specific values will be taken from these curves and used in the summary (Section 9.0).

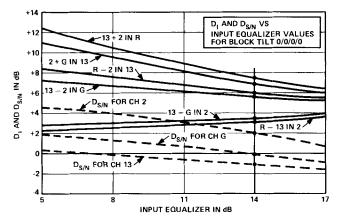


Figure 14.  $D_I$  and  $D_{S/N}$  versus Input Equalizer Values for Block Tilt 0/0/0/0

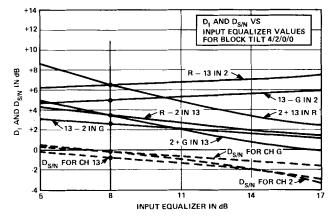


Figure 15.  $D_I$  and  $D_{S/N}$  versus Input Equalizer Values for Block Tilt 4/2/0/0

# 8.0 Normalized Poweramplifier Triple Beat (A $\pm$ B $\pm$ C) Distortion Degradation Factor, D<sub>T</sub>

A  $D_T$  factor for a few sets of  $A \pm B \pm C$  beats are calculated for the  $A_1$  and  $A_2$  specifications and station design parameters given in Section 3.0. The equations used for the  $D_T$  factor calculation are similar to those used for the  $D_I$  factor, with the exception that the relative levels of three frequencies causing a beat interfering with a fourth frequency are determined compared to relative levels of two frequencies causing a beat interfering with a third frequency. The station triple beat product in dB for three frequencies is:

(8.1) T<sub>s</sub> = T<sub>2</sub> + D<sub>T</sub>

Assuming that the only sources of triple beat distortion are  $A_1$  and  $A_2$ :

$$(8.2) \quad 20 \log (t_1 + t_2) = 20 \log [t_2 (1 + t_1/t_2)]$$

 $t_1 = 10 \exp (T_1/20) A_1$  distortion

$$t_2 = 10 \exp(T_2/20) A_2$$
 distortion

The station triple beat distortion can be written as:

(8.3) 
$$T_s = 20 \log (t_2) + 20 \log (1 + t_1/t_2)$$
  
A<sub>2</sub> TB TB Distortion  
Distortion Contributed by A<sub>1</sub>

The ratio of  $A_1$  to  $A_2$  triple beat distortion in dB is:

$$(8.4) \quad T_1 - T_2 = (2) (-G_2 + L_2) + \Delta L + T$$

- where: T is the difference between  $A_1$  and  $A_2$  triple beat product amplitude specification measured at the same flat levels
  - $\Delta L$  is a factor which accounts for the effect of sloped A<sub>1</sub> output levels on T<sub>1</sub>
  - L<sub>2</sub> is the interstage network attenuation at the channel frequency interfered with by the triple beat frequencies

The station triple beat ratio for a set of three frequencies then becomes, using the value of  $(T_1 - T_2)$  evaluated in (8.4).

(8.5) 
$$T_s = T_2 + 20 \log \left[ 1 + 10 \exp \left( \frac{(T_1 - T_2)}{20} \right) \right]$$
  
+  $B_T + 2L_3$ 

The factor  $B_T$  accounts for the effect of any level block tilt at the station output. The factor (2) appears in both equations (8.4) and (8.5) because of the assumption that the triple beat product changes 2 dB for every 1 dB of level change of the three beat producing frequencies. The  $D_T$  factor is:

(8.6) 
$$D_T = 20 \log \left[ 1 + 10 \exp \left( \frac{(T_1 - T_2)}{20} \right) \right] + B_T + 2L_3$$

Values of  $D_T$  for the beat products listed in Table VIII are calculated and listed in Table X in Section 10.

9.0 Normalized Poweramplifier Crossmodulation Distortion Degradation Factor, D<sub>x</sub>

The  $D_I$  and  $D_T$  factors for a given set of channel frequencies are easily calculated, becoming cumbersome only by the number of sets required to describe station performance over its entire passband. These factors do not consider the accumulation

effect of beats at a given frequency. The  $D_x$  factor, however, must include the accumulation of crossmodulation from each channel onto a given channel carrier to be of any use. For the reasons discussed in Section 6.2, the method of calculating nchannel XM by assuming that n-channel XM is (n-1) times two channel XM may not be accurate. However, this calculation method does result in the maximum value of XM distortion for n-channel XM accumulation, if the two channel XM is pure AM (Ref. 6). As has been previously stated, channel 2 XM for one type of IC amplifier (A<sub>1</sub> and A<sub>2</sub>) in common use today, can be analyzed fairly accurately by using the n-1 accumulation rule. Just remember that the following analysis must be applied with good judgment and only after the A<sub>1</sub> and A<sub>2</sub> XM characteristics have been adequately defined by XM measurements.

The  $D_x$  factor for channel 2 is calculated using equations similar to those used for calculation of  $D_T$  (equations 8.1 thru 8.6).

(9.1) X<sub>s</sub> = X<sub>2</sub> + D<sub>x</sub> (One for each channel.)

Assuming that the only sources of XM distortion are  $\mathrm{A}_1$  and  $\mathrm{A}_2.$ 

 $(9.2) \quad 20 \log (x_1 + x_2) = 20 \log x_2 (1 + x_1/x_2)$ 

 $x_1 = 10 \exp{(X_1/20)}$ 

$$x_2 = 10 \exp(X_2/20)$$

The station XM distortion can be written as:

 $(9.3) \quad X_s = 20 \log (x_2) + 20 \log (1 + x_1/x_2)$ 

The ratio of  $A_1$  to  $A_2$  XM distortion is:

- (9.4)  $X_1 X_2 = 2(-G_2 + L_2) + B'_x + D'_x$ 
  - $D'_x$  is the ratio of  $A_1$  to  $A_2$  XM measured at the same flat level
  - same narrows  $B_x$  is a factor accounting for the sloped preamp  $(A_1)$  output levels. The magnitude of this factor varies as a function of input equalizer value and number of channels.
  - $L_2$  is the relative level of the channel for which  $D_x$  is being calculated.

A simplifying assumption is made to reduce the complexity of the  $B'_x$  factor by dividing the sloped  $A_1$  output levels into average level flat blocks as sketched in Figure 16. Calculated

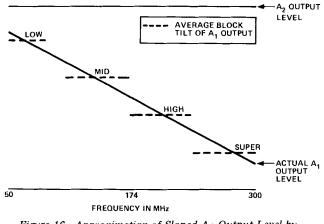


Figure 16. Approximation of Sloped A<sub>1</sub> Output Level by Flat Level Blocks

relative preamp output levels for two input equalizer and block tilt values and the design parameters of Section 3.0 are shown in Figure 17.

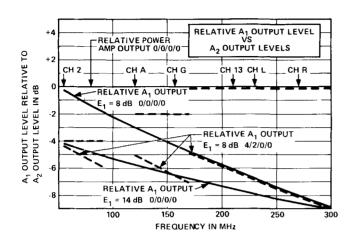


Figure 17. Relative Preamp Output Level versus Frequency

The station XM is now described by:

(9.5) 
$$X_s = X_2 + 20 \log \left[ 1 + 10 \exp \left( \frac{(X_1 - X_2)}{20} \right) \right]$$
  
+  $B_x + 2L_3$ 

The  $B_x$  factor accounts for the effect of any level block tilt at the station output. The factor (2) appears in both equations (9.4) and (9.5) because of the assumption that the XM ratio changes 2 dB for every 1 dB level change of every channel. The  $D_x$  factor is:

(9.6) 
$$D_x = 20 \log \left[ 1 + 10 \exp \left( \frac{X_1 - X_2}{20} \right) \right] + B_T + 2L_3$$

 $D_x$  factor is evaluated for channel 2 using design parameters in Section 3 and listed in Table X of Section 10.

### 10.0 SUMMARY

The D-factors calculated for two station designs, differing only by the values of input and interstage equalizers and two block tilts are summarized in Table X. The station,  $A_1$ , and  $A_2$ parameters used in the calculations are those given in Section 3.0. Note that both station gain distribution (input, interstage and output loss networks) and system block tilt are interrelated and have a very significant effect on the station S/N and distortion.

The station specifications for the design parameters listed in Section 3 and in Table X can now be easily calculated by adding the D-factors listed in Table X to the IC amplifier specifications at the station operating level selected.

Comparison of the two columns of D-factor numbers in Table X, indicates that each design has its strengths and weaknesses. The final design selection requires more extensive analysis of the  $D_T$  factors and also inclusion of measured weighting factors in the analysis to account for the distortion product versus frequency characteristic of the IC amplifiers.

| Table X. | Summary of D-Factors Calculated for Parameters |
|----------|--|
|          | Given in Section 3.0                           |

| D-FACTOR<br>PARAMETERS | INPUT EQU. 14 dB<br>BLOCK TILT<br>0/0/0/0 | INPUT EQU. 8 dB<br>BLOCK TILT<br>4/2/0/0 |
|------------------------|---|--|
| DF                     |   |  |
| 2                      | 12.8                                      | 10.9                                     |
| G                      | 7.7                                       | 6.3                                      |
| 13                     | 5.7                                       | 4.7                                      |
| W                      | 2.8                                       | 2.6                                      |
| D <sub>S/N</sub>       |   |  |
| 2                      | 2.0                                       | 1  |
| G                      | 1   | 7  |
| 13                     | -1.1                                      | 1  |
| W                      | -2.7                                      | -2.5                                     |
| D <sub>1</sub>         |   |  |
| R – 13 in 2            | 3.2                                       | 6.5                                      |
| 13 – G in 2            | 3.6                                       | 5.0                                      |
| 13 – 2 in G            | 5.7                                       | 2.6                                      |
| 2 + G in 13            | 7.0                                       | 3.4                                      |
| 2 + 13 in R            | 7.4                                       | 6.5                                      |
| R – 2 in 13            | 6.0                                       | 3.5                                      |
| DT                     |   |  |
| 3 + 4 + A in 0         | 8.3                                       | -3.8                                     |
| A J + Q in 5           | 4.9                                       | 7.1                                      |
| G + S – J in 13        | 5.3                                       | 3.9                                      |
| 13 + R – J in Q        | 5.3                                       | 5.9                                      |
| 7 – 13 + L in G        | 5.2                                       | 8.7                                      |
| D <sub>x</sub>         |   |  |
| Chan 2                 | 5.9                                       | 5.5                                      |

#### 11.0 CONCLUSION

An analysis method using normalized D-factors for relating the noise and distortion parameters of a fixed gain preamplifier and poweramplifier to the cable repeater trunk station amplifier has been developed. The station design configuration and level tilt limit the noise and distortion performance obtainable from any given fixed gain IC amplifier. Use of the D-factors by the equipment manufacturer, IC manufacturer, and end user provides an aid in analyzing the relationships between IC amplifier performance specifications and trunk amplifier station performance specification. It must be noted that the final station design is determined by combining both measured and analytical results.

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#### SYMBOLS DEFINITIONS

- $A_1$  Fixed gain preamplifier, could be IC or Discrete component design.
- A<sub>2</sub> Fixed gain power amplifier, could be IC or Discrete component design.
- $G_1$  Gain of  $A_1$  in dB
- $G_2$  Gain of  $A_2$  in dB
- G<sub>s</sub> Station Gain
- $F_1$  Noise Figure of A<sub>1</sub> in dB
- $f_1$  Noise factor of  $A_1$ , numeric
- $F_2$  Noise Figure of  $A_2$  in dB
- f<sub>2</sub> Noise factor of A<sub>2</sub>, numeric
- F<sub>s</sub> Noise Figure of Station in dB
- $I_1$  Carrier to second order intermodulation product (A ± B) ratio of  $A_1$  in dB
- I<sub>2</sub> Carrier to second order intermodulation product  $(A \pm B)$ ratio of A<sub>2</sub> in dB
- $I_s \qquad Carrier \ to \ second \ order \ intermodulation \ product \ (A \pm B) \\ ratio \ of \ station \ in \ dB \ for \ given \ I_1, \ I_2, \ station \ design, \ and \\ block \ tilt$
- X<sub>1</sub> Carrier to crossmodulation distortion ratio of A<sub>1</sub> in dB, measured with equal channel levels for given number of channels.
- X<sub>2</sub> Carrier to crossmodulation distortion ratio of A<sub>2</sub> in dB, measured with equal channel levels for given number of channels.

- $X_s$  Carrier to crossmodulation distortion ratio of station for given  $X_1, X_2$  and station design and block tilt.
- $\begin{array}{ll} T_1 & \quad \mbox{Carrier to triple beat product } (A \, \pm \, B \pm C) \mbox{ ratio of } A_1 \mbox{ in } \\ dB & \quad \end{array}$
- $\begin{array}{ll} T_2 & \mbox{ Carrier to triple beat product } (A \pm B \pm C) \mbox{ ratio of } A_2 \mbox{ in } \\ dB \end{array}$
- $\begin{array}{l} T_s \qquad \mbox{Carrier to triple beat product } (A \pm B \pm C) \mbox{ ratio of station} \\ \mbox{ in dB for given } T_1, T_2, \mbox{ station design, and block tilt.} \end{array}$
- $E_1$  dB value of cable loss at reference frequency for which input equalizer equalizes.
- E<sub>2</sub> dB value of cable loss at reference frequency for which interstage equalizer equalizes.
- $FL_1$  Flat loss in dB proceeding preamplifier  $A_1$ .
- $FL_2$  Flat loss in dB in interstage network between  $A_1$  output and  $A_2$  input terminals.
- $L_3$  Flat loss in dB between  $A_2$  (poweramplifier) output and station output.
- L<sub>1</sub> Total loss of input networks, flat loss plus equalizer loss.
- $L_2$  Total interstage loss in dB equal to sum of interstage equalizer loss and flat loss.
- $D_F$  A<sub>1</sub> noise figure F<sub>1</sub> degradation factor for given station design F<sub>s</sub> = F<sub>1</sub> +  $D_F$  in dB.
- $\begin{array}{ll} D_{S/N} & \mbox{Signal to noise ratio degradation factor for given station} \\ \mbox{design. } S_i N_i = 59 + S_i \; (\mbox{ref. frq}) F_1 \; (\mbox{ref. frq}) + D_{S/N} \end{array}$

 $D_{S/N}$  includes  $D_F$ , block tilt factor, signal level variation and noise figure variation across frequency passband.

 $D_I$  A<sub>2</sub> second order IM degradation factor for given station design and I<sub>2</sub>.

 $I_s = I_2 + D_I$  (One  $D_I$  required for each A + B and A - B product).

 $D_T \qquad A_2 \ third \ order \ (triple \ beat) \ degradation \ factor \ for \ given station \ design \ and \ T_2.$ 

 $T_s$  =  $T_2$  +  $D_T$  (One  $D_T$  required for each A  $\pm$  B  $\pm$  C product).

 $D_x$  A2 crossmodulation degradation factor for given station design and channel.

 $X_s = X_2 + D_x$ 

- $B_T$  Block tilt factor relating difference, in dB, of third order (triple beat) product magnitude measured at block tilted levels compared to the magnitude measured at flat levels. Each A  $\pm$  B  $\pm$  C product has a  $B_T$ .